

## Analysis of Changes in Tension in Leading Branch Belt Drive

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### Abstract

This paper presents method of determination in the regularity change in the branches of a belt drive with an eccentric tensioning roller. On the basis of analysis in the research results identified the recommended belt transmission parameters.

**Keywords:** Belt drive; Tension; Roller; Extension; Leading branch; Voltage; Fluctuation; The moment; Resistance

### Introduction

On a number of technological machines, in particular of small cotton cleaners litter is important in kolkova drum rotation angular speed of a variable at a certain frequency and amplitude, allowing effect intensification cotton cleaning [1,2].

Therefore, in the drive of the machine used belt transmission with belt tension [3]. Thus in the belt drive (Figure 1) is mainly driven pulley is rotated at variable angular speed.

The theoretical task of the problem: In the process of transmission branches are extended on the values depend on the change of angular speeds pulleys. According to the work of the branches in the belt drive extension determined from the expression:

$$\Delta l_1 = \Delta \sigma_1 \left[ \frac{1}{E} + \frac{D_2}{2fE} (1 - e^{-f\phi_0}) \right],$$

$$\Delta l_2 = \Delta \sigma_2 \left[ \frac{1}{E} + \frac{D_1}{2fE} (e^{-f\phi_0} - 1) \right] \quad (1)$$

Where,  $\Delta \sigma_1, \Delta \sigma_2$  - changes in belt stress transmission branches Pa; E- modulus belt, Pa;  $D_1, D_2$  - the diameters of the guiding and driven pulleys, mm; f- the coefficient of friction of the belt on the pulley surface;  $\phi_0$  - elastic slip angle. Furthermore, lengthening pulleys branches can be determined by the angular displacement of pulleys:

$$\Delta l_1 = (D_1\varphi_1 - D_2\varphi_2),$$

$$\Delta l_2 = (D_2\varphi_2 - D_1\varphi_1) \quad (2)$$

Thus according to Figure 1 can be determined

$$l_2 + \Delta l_2 = l_2' + \Delta l_2' + R_p \sin \alpha + l_2'' + \Delta l_2'' \quad (3)$$

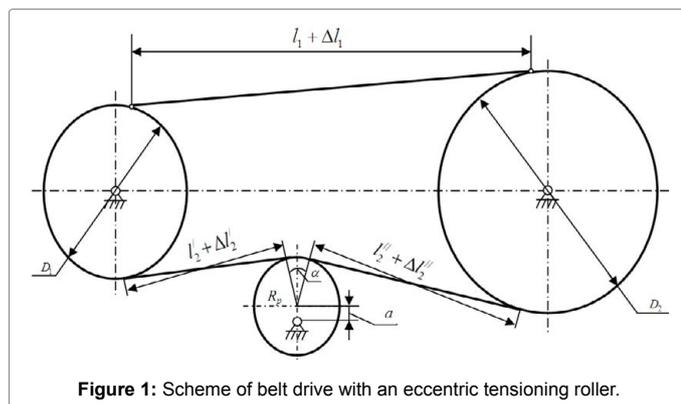


Figure 1: Scheme of belt drive with an eccentric tensioning roller.

$$\text{or } \Delta l_2 = \Delta l_2' + \Delta l_2''$$

Differential equations describing the motion of the belt drive pulleys are of the form

$$J_1 \frac{d^2 \varphi_1}{dt^2} + \frac{k_3 F D_1^2}{4} \varphi_1 - \frac{k_3 D_1 D_2 F}{4} \varphi_2 = M_g,$$

$$J_2 \frac{d^2 \varphi_2}{dt^2} - \frac{k_3 D_1 D_2 F}{4} \varphi_1 + \frac{k_3 D_2^2 F}{4} \varphi_2 = M \sin \omega t \quad (4)$$

$$\text{Where, } k_3 = (k_1 + k_2) \frac{1}{k_1 k_2}; \quad k_1 = \frac{1}{E} + \frac{D_2}{2fE} (1 - e^{-f\phi_0});$$

$$k_2 = \frac{1}{E} + \frac{D_1}{2fE} (e^{-f\phi_0} - 1), M_g = M_1 \sin jt.$$

$M_g$ -drive moment to the drive pulley shaft,  $M_1 M_0$  -the amplitude hesitation of the driving and disturbing moments. Decision of system (4) differential equations belt drive found in the form:

$$\varphi_1 = \varphi_{10} \sin \omega t, \varphi_2 = \varphi_{20} \sin \omega t \quad (5)$$

Supplying (5) with respectively, in the equation (4) we obtain the expression for determining the values the amplitudes ripple of the belt drive pulleys

$$\varphi_{10} = \frac{A}{B} \left[ \frac{B \left( \frac{M_1 \sin jt}{\sin \omega t} + J_1 \omega^2 \right) + A (J_1 \omega^2 + M_0)}{A^2 - B^2} \right] - \frac{J_2 \omega^2 + M_0}{B},$$

$$\varphi_{20} = \frac{B \left( \frac{M_1 \sin jt}{\sin \omega t} + J_1 \omega^2 \right) + A (J_1 \omega^2 + M_0)}{A^2 - B^2} \quad (6)$$

$$\text{Where, } A = K_3 \frac{D_1^2 F}{4}; B = K_3 \frac{D_1 D_2 F}{4}$$

When this tension will change

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$$\Delta\sigma_{10} = \frac{R_1\varphi_{10} - R_2\varphi_{20}}{k_1}$$

$$\Delta\sigma_{20} = \frac{R_2\varphi_{20} - R_1\varphi_{10}}{k_2} \tag{7}$$

Then, full of tension in the branches of a belt drive get

$$\sigma_1 = \sigma_{10} + \Delta\sigma_{10} \sin \omega t$$

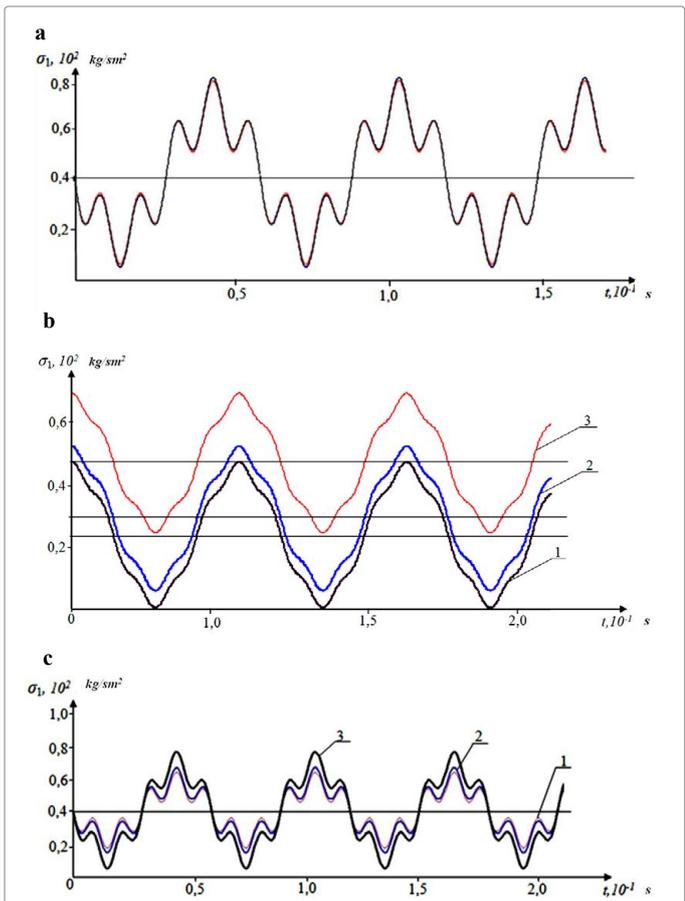
$$\sigma_2 = \sigma_{20} + \Delta\sigma_{20} \sin \omega t \tag{8}$$

**Analysis of the Results of the Numerical task of the Problem**

Numerical solution and analysis of results in  $\sigma_1$  and  $\sigma_2$  changes implemented under the following initial values of the parameters belt drive with variable gear ratio:

$R_1=1,5 \cdot 10^{-3} m$ ;  $R_2=2,0 \cdot 10^{-3} m$ ;  $I_1=0,02 kgm^2$ ;  $I_2=0,033 kgm^2$ ;  $F=2,5 sm^2$ ;  $\sigma_0=22 kg/sm^2$ ;  $\omega = 0,75 p_2$ ;  $\sigma_{10}=40 kg/sm^2$ ;  $\sigma_{20}=40 kg/sm^2$ ;  $M_0=25 Nm$ ;  $E=12 \cdot 10^2 kg/sm^2$ ;  $l=0,185 \cdot 10^{-3} sm$ ;  $M_1=8,5 Nm$ .

Figure 2 shows a graphic pattern of the belt tension changes in the



Where,  
 a-before  $\sigma_{10}=0,9 \cdot 10^2 kg/sm^2$   
 b-before  $\sigma_{10}=0,28 \cdot 10^2 kg/sm^2$  (1- curve); before  $\sigma_{10}=0,33 \cdot 10^2 kg/sm^2$ (2- curve); before  $\sigma_{10}=0,54 \cdot 10^2 kg/sm^2$ (3- curve)  
 c-before  $\sigma_{10}=0,4 \cdot 10^2 kg/sm^2$ ; 1- $M_0=19,5 Nm$ ; 2- $M_0=25,0 Nm$ ; 3- $M_0=28,5 Nm$ .

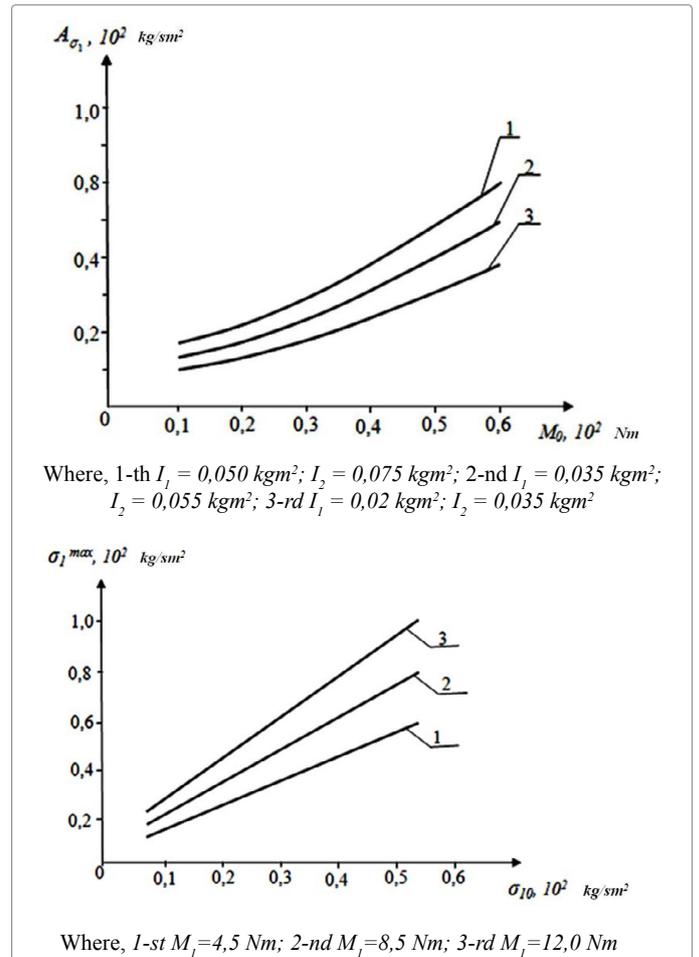
**Figure 2:** Laws of change of tension in the leading branches of the belt drive from time to time  $\sigma_1$  fluctuations.

leading branches on the transfer at  $\sigma_{10}=40 kg/sm^2$   $M_1=5,2 Nm$ ,  $M_0=18 Nm$ .

Analysis of the resulting pattern shows that the amplitude of the low component match, depending on the disturbing  $M_0$  resistance force and frequency  $\omega$ , high-frequency components is dependent on the value of  $M_1$  and  $j$ .

The amplitude of the ripples reaches  $0,373 \cdot 10^2 kg/sm^2$ , low frequency rippling occur in the range of  $(9,0 \dots 11)s^{-1}$ . It should be noted that the value of  $\sigma_{10}$  not affect the nature of the change in time  $\sigma_1$  in time (Figure 2b). Thus, from the graphs in Figure 2b. It is seen that the graphs 1, 2 and 3 are shifted in parallel relative to the axis t. Figure 2 presents the patterns of change in  $\sigma_1$  changing  $M_0$  and  $\sigma_{10}=40 kg/sm^2$ .

From the graphs show that the variation of  $\sigma_1$  actually is not treason. However, the amplitude changes Based on the results of processing graphics are constructed according to the changes in the leading branches of the belt  $M_0$  changes in ripple fluctuation amplitude variations at the moment of inertia in pulleys, which are shown in Figure 3a. Analysis of the relationship shows that the moment of inertia in pulleys  $I_1=0,02 kgm^2$  and  $I_2=0,035 kgm^2$  with an increase in the amplitude of the resistance torque values from  $0,12 \cdot 10^2 Nm$  before  $0,56 \cdot 10^2 Nm$  voltage oscillation amplitude in the lead belt branches



Where, 1-th  $I_1 = 0,050 kgm^2$ ;  $I_2 = 0,075 kgm^2$ ; 2-nd  $I_1 = 0,035 kgm^2$ ;  $I_2 = 0,055 kgm^2$ ; 3-rd  $I_1 = 0,02 kgm^2$ ;  $I_2 = 0,035 kgm^2$

Where, 1-st  $M_1=4,5 Nm$ ; 2-nd  $M_1=8,5 Nm$ ; 3-rd  $M_1=12,0 Nm$

**Figure 3:** Graphic changes depending on the amplitude of the vibrations on the belt tension in the leading branches of the transmission changes in amplitude on the disturbing force to the driven pulley (a) and the maximum belt tension on the voltage variation of the pre-tensioning of the belt (b).

increasing from  $0,115 \cdot 10^2 \text{ kg/sm}^2$  to  $0,38 \cdot 10^2 \text{ kg/sm}^2$  for nonlinear patterns.

When  $I_1=0,050 \text{ kgm}^2$  and  $I_2=0,075 \text{ kgm}^2$   $A_{\sigma_1}$  increases to  $0,785 \cdot 10^2 \text{ kg/sm}^2$ .

It is common knowledge the amplitude of the disturbing moment increases the deformation of the belt, and by the tense Ascending. Besides the increase in the moments of inertia of pulleys in the variable driving modes lead to cyclic changes in load in the branches of a belt drive (Figure 3a). Therefore, the recommended value is  $I_1=(0,03...0,04) \text{ kgm}^2$  and  $I_2=(0,05...0,06) \text{ kgm}^2$ .

Increased tension  $\sigma_{10}$  at the amplitude of the disturbing drive torque  $M_1=12,0 \text{ Nm}$  leads to an increase  $\sigma_1^{max}$  from  $0,426 \cdot 10^2 \text{ kg/sm}^2$

to  $1,48 \cdot 10^2 \text{ kg/sm}^2$ , and  $M_1=4,5 \text{ Nm}$  maximum value of the voltage fluctuations in the leading branches of the transmission It comes only to  $0,93 \cdot 10^2 \text{ kg/sm}^2$ .

It is common knowledge that driving with increasing force values and accordingly increases the belt tension deformation particularly in the leading branch, which transmits the motion from the driving pulley to the driven (Figure 3b). Figure 4 shows the pattern of the belt voltage fluctuations in the leading branches of the transmission by varying the values of  $\omega$ ,  $j$ ,  $M_1$  and  $M_0$ . An analysis of the laws shows that with the change in the frequency of the driving values of  $j$  and the frequency  $\omega$  resistance on the shaft of the driven pulley is also changed form  $\sigma_1$  voltage fluctuations in the leading branches of the belt drive.

At the same time with the increase in  $M_1$  and  $M_0$  increases the amplitude of the fluctuations  $\sigma_1$  as the high-frequency and low-frequency components (Figures 4a and 4b). It should be noted the phase shift with increasing fluctuations  $\sigma_1$   $j$  with respect to  $\omega$ .

### Conclusion

An analytical method for determining the laws of the belt voltage fluctuations in the leading branches of the belt drive with tensioning roller. Substantiates the numerical values of the parameters in the belt transmission.

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