Euclidean Norm in Composite Severity Score to Evaluate an Allergic Reaction from Conjunctival Provocations

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Abstract

A simple and robust estimation method is suggested to outline the severity of an allergic reaction from several conjunctival challenges combined in one diagnostic procedure — conjunctival provocation test (CPT). The CPT is performed by a stepwise application of an allergen solutions of increasing concentrations onto the patient’s conjunctiva. The allergic reaction is estimated after each application by a numerical severity score. The severity scores are combined into one composite value, using their Euclidean norm divided by the square number of applications. The difference of the composite scores before and after the therapy is proposed as an appropriate outcome parameter in drug registration trials to represent the therapeutic effect. Applicability of the suggested method is shown in a randomized controlled double-blind dose-finding study of 150 patients with birch pollen allergy. The superior effect of the highest doses over the lowest dose for this study was not found to be statistically significant (p<0.1 in U-test).

Keywords: Allergy diagnosis; Conjunctival provocation; Severity score; Composite score; Allergic rhinoconjunctivitis

Introduction

The conjunctival provocation test (CPT) is a diagnostic procedure for testing airborne allergens causing allergic rhinoconjunctivitis [1,2]. It has been thoroughly evaluated with regard to its precision [3] and compared with nasal provocation tests [4]. Nowadays, the CPT is used for evaluation of allergic rhinoconjunctivitis [5,6] and is accepted by regulatory authorities as an outcome parameter in dose-finding trials.

The CPT consists of several conjunctival challenges with increasing allergen concentrations. Each challenge is an instillation of the ophthalmic solution containing an allergen. The conjunctiva allergic reaction is assessed after each challenge by the numerical score. If the score is equal or higher than the threshold value, the CPT stops. In the considered clinical study the allergic reaction to each challenge was assessed in terms of severity scores 0 ≤ s ≤ 4, by use of the Gronemeyer’s grading scale [4,7], presented in Table 1. The CPT was performed with a maximum of three allergen challenges (1 ≤ i ≤ 3). The used diluted allergen solutions are: 100, 1000 and 10 000 SQ-E/ml (‘ALK-lyophilized SQ’, ALK Abell’ø A/S, Hørsholm, Denmark) for first, possible second and third challenges, respectively.

The CPT steps are:

1. Before challenge, the right (control) eye is treated with a diluent without an allergen to reveal possible non-allergic reaction. If control reaction is positive, the patient is excluded from the study.

2. If control reaction is negative, a single drop of allergen solution with the lowest titration, 100 SQ-E/ml, is put into the left (provocation) eye. If the assessed severity score is s1 ≥ 2, the allergic reaction is positive and the CPT is complete. Here, the number of challenges to reach a positive reaction is n=1.

3. If the allergic reaction to 100 SQ-E/ml is negative (i.e. s1<2), the solution with the next higher concentration, 1000 SQ-E/ml, is applied. If s2 ≥ 2, the positive CPT result is reached at n=2.

4. If the reaction to 1000 SQ-E/ml results in s2<2, a drop with the highest concentration 10 000 SQ-E/ml is applied. If the CPT is negative to application of 10 000 SQ-E/ml, the patient is excluded from the study. Otherwise the positive CPT result is reached at n=3.

When accessing the reactive threshold only, non-zero information derived from challenges at lower concentrations is lost. For an accurate comparison of the allergic severity before and after the treatment, one should take into account non-zero severity scores of lower challenges, where the threshold value is still not reached and some allergic symptoms are already obviously observed. Therefore, it is suggested to estimate the severity with the composite score.

Method

The CPT is considered to be positive and complete, if the severity score s1 is equal or greater than the threshold value s(i)=2. Here, i is the challenge number, 1 ≤ i ≤ 3. The composite score C(i) is calculated for the j-th patient (1 ≤ j ≤ N) as an Euclidean norm of severity scores s1, s2 and s(i)

\[ C(i) = \sqrt{s_1^2 + s_2^2 + s(i)^2} \]

Table 1: Gronemeyer’s grading scale to assess allergic severity in CPT [4]. Threshold value for positive CPT is 2.

<table>
<thead>
<tr>
<th>Severity score (i)</th>
<th>Description of the severity</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Stage 0: no subjective or visible reaction</td>
</tr>
<tr>
<td>1</td>
<td>Stage 1: itching, reddening, foreign body sensation</td>
</tr>
<tr>
<td>2</td>
<td>Stage 2: stage 1+tearing, vasodilation of conjunctiva bulbi (threshold value)</td>
</tr>
<tr>
<td>3</td>
<td>Stage 3: stage 2+vasodilation and erythema of conjunctiva tarsi, blepharospasms</td>
</tr>
<tr>
<td>4</td>
<td>Stage 4: stage 3+chemosis, lid swelling (did not occurred during this study)</td>
</tr>
</tbody>
</table>

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Table 2: Composite score \( C_j \) of the \( j \)-th patient, calculated by Equation 1 for all possible combinations of the assessed severity scores, according to the grading conditions, used in the described study.

<table>
<thead>
<tr>
<th>( n=1 )</th>
<th>( n=2 )</th>
<th>( n=3 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

\[
C_j = \sqrt{\sum_{i=1}^{s_j} S_i^2} / n^2
\]

At a maximum of three challenges, at \( 0 \leq s_j \leq 4 \) and at \( s_m=2 \), Equation 1 conforms to the following two requirements:

- Each combination of the \( s_i \) results in a unique \( C_j \).
- The decreasing \( C_j \) value indicates an improvement of allergic severity (hypensensitisation). The \( C_j \), calculated for all possible \( 0 \leq s_j \leq 4 \) with \( s_m=2 \) and \( 1 \leq n \leq 3 \), are presented in Table 2.

A mean of the composite score at "time-x" for a group of \( N \) (tx) patients is:

\[
\overline{C}(tx) = \frac{\sum_{j=1}^{N(tx)} C_j(tx)}{N(tx)}
\]

The change of the mean composite score between "time-0" and "time-1" represents the therapeutic effect:

\[
\Delta C = \overline{C}(0) - \overline{C}(1)
\]

The number of patients participating in the CPT study at "time-1" \( N(t1) \) can be smaller than the number of patients at "time-0" \( N(0) \) if someone drops out before the visit at "time-1". To avoid bias only patients tested both at "time-0" and at "time-1" must be considered, i.e. \( N(tx) \) in Equation 2 must be \( N(0) \cap N(1) = N(t1) \). However, the number of challenges can change for some patients at "time-1" in a positive or negative direction. In order to estimate fluctuations \( \phi \) induced by changes in the number of challenges for some patients, the following procedure is suggested:

1. The difference of the single score is calculated for each \( j \)-th patient:

\[
\Delta S_{i,j} = S_i^{(0)} - S_i^{(1)}
\]

Here, \( j \) denotes those patients, who were tested both at "time-0" and at "time-1", i.e. \( 1 \leq j \leq N (1) \).

2. The value \( \Delta_{C,j} \) is introduced for each \( j \)-th patient. It is calculated as an Euclidean norm of \( \Delta S_{i,j} \), divided by the square minimal number of challenges \( n^2 \), \( n=\min(n(\text{Max}), n(\text{Min})) \), taking into account the sign of each \( \Delta_{S_{i,j}} \):

\[
\Delta_{C,j} = \frac{\sum_{i=1}^{n(\text{Min})} \text{sgn}(\Delta S_{i,j}) \cdot (\Delta S_{i,j})^2}{n^2}
\]

3. For a group of patients \( N(t1) \) the arithmetic mean of the \( \Delta_{C,j} \)-values is:

\[
\overline{\Delta C} = \frac{\sum_{j=1}^{N(t1)} \Delta_{C,j}}{N(t1)}
\]

4. The maximal fluctuation \( \phi_{\text{Max}} \) is defined as an absolute difference of values calculated in Equations 3 and 4:

\[
\phi_{\text{Max}} = |\overline{\Delta C} - \overline{C}|
\]

Results

The therapeutic effect obtained in a randomized controlled double-blind dose-finding study of 159 patients with birch pollen allergy is presented in Figure 1. Here, quantitative values of the triangle data points, connected with a solid line, are calculated by Equations 1–3 for 150 patients, which have participated all study visits. The triangles show the therapeutic effect, as a change in the mean composite score \( \Delta C \), for four groups of patients treated with the medicament in four different doses M1–M4, respectively. The dots connected with the dashed line in Figure 1 indicate the qualitative success of the therapy for the M1–M4 treatment groups. This qualitative estimation represents the normalized number of patients in each M1–M4 group, whose symptoms are improved. The normalization factor is 123 (82% of 150)–number of patients with improved symptoms in all treatment groups. The CPT was carried out before and after the treatment. Error bars of the quantitative values, shown by the triangle points represent statistical errors of the mean and the error bars of the qualitative dot
The developed method for calculating a composite score of several individual measurements, each resulting in a single score $0 \leq s_i \leq 3$, was successfully applied in the estimation of the therapeutic effect in this dose-finding study in allergy. The method is planned to be used as standard in analysis of the next clinical studies in allergy with conjunctival provocation.

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References