The Informational Loadings of a Stock

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Abstract

In this short paper, I selectively review some recent developments related to the idea that jumps in stock prices incorporate the most valuable information, and thus the quantification of a stock’s exposure to jump events is important for financial risk management and portfolio construction. There are two main methodologies of estimating jump betas: a) the more widely used high or ultra high frequency procedures that rely on the asymptotic behavior of elaborate and sophisticated econometric constructs, such as the bi-power variation or local averaging techniques in order to isolate market microstructure noise at high frequencies, and b) very recently a new non-parametric skew-based methodology that does not rely on the use of high frequency data and is thus immune to market microstructure noise.

Keywords: Stock beta; Price jump; Noise trading; Information in stock prices; Return skew; Market co-skew; Information-loading

JEL Classification: G12

Introduction

The use of diffusion based asset pricing theories in pricing real world financial assets presents a major challenge for economists and financial experts. Calibrating diffusions to real price data and in particular derivatives’ prices, even if we allow for stochastic volatility, has proven a particularly difficult task. One of the reasons of such difficulty in fitting real stock return and option price data to most models is that real prices seem to exhibit exposure to extreme moves (excess kurtosis) and asymmetry (skew) in ways that do not seem easy to comprehend. In such an environment an investor who exhibits skew preference can improve the mean-variance profile of an asset by “selling” its return skew either through dynamic trading or using option based strategies. Leland [1] argues that the classical beta does not account for skew and should be replaced by \( \frac{\text{cov}(R, R^n)}{\text{cov}(R, R^n)} \) with \( b \) the “market price of risk” for a power utility investor.

Evidence of jumps that help better explain the higher moments of asset returns, namely excess kurtosis and skew, is now widely recognized. Merton [2] recognized that theories developed for continuous path dynamics such as Black and Scholes option pricing will have to be modified in order to explain how risk averse agents demand continuous path dynamics such as Black and Scholes option pricing will be recognized. Merton [2] recognized that theories developed for asset returns, namely excess kurtosis and skew, is now widely recognized.

The High Frequency Approach

In recent years, due to advances in information technology, we have witnessed the move away from a manned trading floor towards completely electronic trading largely devoid of human intervention (Straight-through processing). This move has generated the availability of databases consisting of observations sampled at ultra-high frequency up to every second, and thus facilitated an extensive research program\(^2\) that takes advantage of high frequency data. When the econometrician is endowed with ultra-high frequency data, it is tempting to try to isolate the jumps as moves greater than a specific value (say 1%). In a significant contribution to the literature Barndorff-Nielsen and Shephard [4,5] study two natural measures of the realized within-day price variance, the well known day (t) Realized Variance that measures the summed quadratic log-returns \( R_t^2 = \sum r_j^2 \) and the novel realized Bipower Variance that measures summed neighboring log return cross-products \( \sum r_j r_{j+1} \). Time is measured in daily units for integer \( t \), and for an N partition of the \( t \)° day, we denote the within-day log-returns \( r_j = \frac{P_{t+j-1} - P_{t+j}}{P_{t+j-1}} \). The significant and intuitive finding is that, under reasonable assumptions about the stock price dynamics, when the fineness of the partition tends to infinity, the two measures

\[^2\text{See for example Pan [10], Eraker [11] and references therein.}\]

\[^3\text{Huang and Tauchen [12], Jiang and Oomen [13], Lee and Mykland [14], Todorov and Bollerslev [15], Lee and Hannig [16], Lee [17].}\]
have different limits, with \( \lim_{N \to \infty} RV_t \) and \( \lim_{N \to \infty} BV_t \) respectively including and not including jump activity. This allows us to quantify jump activity through the difference between the two measures.

The High and Ultra-High Frequency methods are promising and are quite attractive among researchers and practitioners. Yet, and despite their attractiveness, there are many practical issues related to their implementation that limit our ability to calibrate them to real data and challenge their true practicality and robustness: a) The most important problem is that usually High Frequency methods don’t retain power when applied to the noisy high frequency data. B) When applying High and Ultra-High Frequency methods, one has to determine the rejection regions for claiming jump arrivals; i.e. determine the cut-off value that constitutes a jump move. For example, will this value be 1% or 1.2%? This is a difficult question to answer without first imposing some restrictive (and potentially unjustified) assumption about the underlying distributions for the noise variance, the underlying return process volatility, the jump arrival intensity, and the distribution of jump sizes. Even when jumps are detected in a particular period (say 15 min) one cannot reasonably assume that the entire price move is due to the jump. That means that even when we are relatively confident a jump has occurred, we still need to decide what part of what returns constitutes the jump and what part is due to the ever present diffusive noise. One faces the dilemma of how fast to sample the TAQ database. One can seemingly increase the power of tests by increasing the frequency of observations over a fixed time interval. Faster sampling (say at 5 min intervals) allows for easier jump detection but at the same time increases the noise due to market microstructure and in particular the so called bid-ask bounce. Slower sampling (at say 30 min intervals) takes care of a large part of the market microstructure noise but increases the need to make unjustified parametric assumptions about the underlying jump sizes’ distribution, intensity of arrival and so on.

**The Skew-Based (Low Frequency) Approach**

In this section we present some ideas behind the method developed in Polimenis [6] that does not rely on high frequency data and is thus immune to market microstructure effects. According to that paper the cumulative effects of same-sign market wide jump activity during the investing period should be understood as unobservable information factors (i-factors) for the market. The loadings of individual stocks to these factors quantify exposure to significant market risks and constitute a set of new risk measures that aim at filtering away trading noise from information arrival. According to this concept, noise evolution occurs in continuous time along a continuous price path, while new observations over a fixed time interval. Faster sampling (say at 5 min intervals) allows for easier jump detection but at the same time increases the noise due to market microstructure and in particular the so called bid-ask bounce. Slower sampling (at say 30 min intervals) takes care of a large part of the market microstructure noise but increases the need to make unjustified parametric assumptions about the underlying jump sizes’ distribution, intensity of arrival and so on.

The model for the \( i \)th stock return then becomes

\[
\Delta p(dt) = \alpha_i dt + \beta_i w(dt) + \gamma_i y(dt) - \delta_i z(dt) + e_i(dt)
\]

with \( \beta_i \) the individual stock loading on the diffuse market noise, and the idiosyncratic stock specific noise

\[
e_i(dt) = q_i w(dt)
\]

In this setup, total stock variance (energy) \( \sigma^2 \) is decomposed into the diffuse systematic variance (noise) \( \beta_i^2 \sigma^2 \), the systematic jump variance (signal) \( \gamma^2 \sigma^2 \), and the idiosyncratic (again noise) variance \( \delta_i^2 \).

The problem in identifying the jump loadings is that assuming that we can observe the \( Y \) and \( Z \) processes separately is unrealistic; in most cases we observe only the full market return in discrete times. The main idea in Polimenis [6] is the development of a set of universal co-skew conditions that can be used to quantize the degree of exposure of individual stocks to the latent jump risk factors. Skew and co-skew are high order cumulants and “blind” to Gaussian noise, whereas covariance based statistics are not. For example, the classical beta \( \sigma_{im} / \sigma_{mm} \) of running a regression of \( \Delta p \) against market returns \( \Delta m \) wrongly assumes a single factor risk, and depends only on the breakdown of the total quadratic variation into its individual components and thus does not carry path specific jump information

\[
b = \frac{\sigma_{im}}{\sigma_{mm}} = \frac{\sigma^2_m + \sigma^2_w}{\sigma^2_m} \beta_i + \frac{\sigma^2_y}{\sigma^2_m} \gamma_i + \frac{\sigma^2_z}{\sigma^2_m} \delta_i.
\]

On the other hand the noise parameters do not participate in the co-skew of \( \Delta p \) to \( \Delta m \)

\[
\sigma_{mn} = \gamma_i \beta_i - \delta_i \delta_i.
\]

Consequently, skew-based methods improve the "signal-to-noise" ratio of our estimates. The paper uses this idea to develop a non-parametric set of skew conditions that can be used to help identify the magnitude of the latent jump components, and furthermore, the degree of exposure of individual stocks (the loadings) to such risks. According to Polimenis (2012), once we view the Gaussian part of the price path as noise, we need to shift our attention to skew rather than variance as the most significant moment.

Skew and co-skew estimates are quite sensitive to extreme realized values, and the robustness of the technique is further investigated in Theodosioud, et al. [8]. More recently Polimenis and Papantonis [9] extend the methodology and propose to make it more robust through the estimation of the jump betas for two stocks jointly. They observe that the requirement that the individual stock skew is exactly matched is placing a burden on the estimation system, and argue that when...
this restrictive requirement is relaxed in a joint framework the system calibrates to more robust solution revealing information about the level of idiosyncratic skews. Under this system the idiosyncratic component becomes

\[ e(dt) = u(dt) + q_w(dt) \]

where \( u(dt) \sim (0, dt) \) is the pure jump idiosyncratic info. Allowing for stock jumps that are not simple transmission of market jumps but directly related to the underlying stock is a realistic assumption.

**Conclusion**

Measuring a stock's exposure to jumps is important for financial risk management and portfolio construction. This is a fascinating and technically challenging area of ongoing research. The purpose of this short review paper is to stimulate a debate as to the potential merits of the high frequency methods on one hand and the skew based frequency neutral methods on the other hand. Due to the limited space, only a few papers focused on jump and jump-beta estimation are discussed, so the paper does not in any way claim to be a thorough review paper.

**References**