Variable-Temperature Measurements of the Dielectric Relaxation Spectroscopy in 0.1 SiO$_2$-0.2 CaO-0.2 Na$_2$O-0.5 P$_2$O$_5$ Bioactive Glass Materials

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Abstract

Bioactive glasses with chemical composition 0.1 SiO$_2$-0.2 CaO-0.2 Na$_2$O-0.5 P$_2$O$_5$ have been prepared. The dielectric properties of the samples were measured in the frequency range from 100 Hz to 1 MHz and temperatures range from 100 to 370 K ($T_g = 400$ K). The obtained data were analysed by the means of dielectric permittivity representation and modelled using the Havriliak–Negami equation. Various relaxation parameters were calculated with accuracy. Furthermore, investigation of the temperature dependence of their relaxation time using the Vogel–Tammann–Fulcher (VTF) model shows the weak interaction between alkali ions constituents and molecular network-formers for temperatures up to the glass transition.

Keywords: Amorphous materials; Composite; Chemical synthesis; Differential Scanning Calorimetry (DSC); Dielectric properties; Impedance spectroscopy electrical properties

Introduction

In the recent years, there is increasing demands of using and understanding bioglass materials for scientific research and industrials [1]. Silicate and phosphate glasses have been carried out with the aim to control physical, chemical and biological properties, such as second-order nonlinear optical susceptibility and bioactivity, they have also found application as biomaterials to replace or repair hard or soft tissues [2-5]. Phosphosilicate based glasses produce a bonelike apatite layer on its surface when interacting with host medium [6-8]. Recently, researchers have been focusing on the bioactive phosphate glasses because they are unique class of materials that are biodegradable and biocompatible, and their degradation can be tailored for varying from days to several months as bone implant by changing the glass modifiers and preparation techniques [9,10]. By suitably altering the composition, the glass network modifier oxides like CaO and Na$_2$O are added to phosphosilicate composite network in order to improve its electrical transport properties and to control the degree of solubility of bioactive glass in a physiological environment [11]. Further, the solubility of the bioactive glass has been directly linked to the ionic release from the material to the host medium. Hence the understanding of the alkali ion transport mechanism of the bioglass is very important. The dynamics of charges can be studied by analytical technique of alternating current impedance spectroscopy which has been considered as the best tool for understanding the dynamics of alkali ions in the bioactive glass [12]. The real and imaginary parts, of the dynamics modulus formalism and complex impedance representation of phosphate-silicate bioactive glass has been studied, respectively, by Mai et al. and Mariappan et al. they suggest that the observed relaxations in the bioactive glass may be more appropriately considered as an intrinsic property of the non-periodic arrangement of atoms or ions in a solid than as being due to the diffusion of specific types of ions in it [13,14].

Dielectric relaxation and related phenomena are present in this bioactive glass and their investigation is essential not only from the practical point of view due to the potential application, but also for the insight information that can provide referring to molecular/ions mobility, polarization and conductivity mechanisms [15-17]. These amorphous bioactive glasses are formed by the mixture of the merit compositions of silicate-phosphate as a network formers and sodium-calcium network modifiers powders which are considered as disordered system and many equations have been proposed for describing their behavior in terms of the permittivity of their constituents.

The aim of this study was to investigate the dielectric relaxation behaviour and electrical mobility of the phosphosilicate bioglass composite containing 0.1 SiO$_2$-0.2 CaO 0.2 Na$_2$O-0.5 P$_2$O$_5$ and to their modelling. The relaxation phenomenon exhibited by the sample in the range from 100 Hz to 1 MHz was studied as a function of the temperature below the glass transition point $T_g$. In order hand, it is known that glass-forming materials are characterized by a number of unusual properties, which seem to be inherent to the glassy state of matter and which are quite universally found in such different types of materials [18-20]. May be the most prominent examples are the non-exponential time dependence of their relaxation behaviour and the non-Arrhenius temperature dependence of their structural relaxation dynamics [21]. Furthermore, there are numerous competing theoretical models of the glass transition that can describe the observed behavior with various levels of precision and the glass-physics community still is far from reaching any consensus in the settlement of this question [22-24].

In our case and in order to parameterize the obtained results on the temperature-dependent relaxation, we revert to the most prominent
Vogel-Fulcher-Tamman (VFT) law phenomenological approach [25].

Experimental Techniques

Sample preparation

Sample of phosphosilicate bioactive glass with chemical composition 0.1 SiO2-0.2 CaO-0.2 Na2O-0.5 P2O5 was prepared from Na2CO3 (99.98%), CaCO3 (100%), SiO2 (99.9%) and (NH4)2HPO4 (99.8%) powders. Initially, they reagents (NH4)2HPO4, Na2CO3 and CaCO3 were kept in an oven and tried at 400 K for 12 hours in order to remove any traces of water and absorbed gases CO2 and NO2. Then stoichiometric amounts of the starting materials were weighed by using digital electronic balance and were ground in a gate mortar for a few minutes. The mixtures were placed in alumina crucible and melted in an electric furnace at 1100 K for one hour. After complete homogenization, the melt was poured into preheated stainless steel mold with a cylindrical shape.

Measurements

Differential scanning calorimetry (DSC) measurement was performed on a DSC121M Rudolph Instruments, with a heating rate of 10°C/min. For the dielectric measurements, the sample were prepared as a disc with a thickness of about 1 mm. Aluminium electrodes of 10 mm diameter were deposited on the opposite sides of the samples. The electrical leads were fixed by silver paint. The dielectric measurements were carried out, in the frequency range from 100 Hz to 0.2 MHz, using a SR850 DSP Lock-In Amplifier, in the typical lock-in configuration. We used the “in-phase” (Vf) and the “out-of-phase” (Vq) components of the measured signal, and then we calculated the real and imaginary parts of the complex impedance Z*(ω), using the expressions:

\[ Z'(\omega) = \frac{R(V_f V_q - V_i^2 - V_q^2) - \omega C^2 R^2 V_f V_q}{(1 + \omega C^2 R^2)} \]  \[ Z''(\omega) = \frac{V_f V_q R + \omega C^2 R^2 (V_f V_q - V_i^2 - V_q^2)}{(1 + \omega C^2 R^2)} \]  \[ Z^*(\omega) = \frac{V_f V_q R + \omega C^2 R^2 (V_f V_q - V_i^2 - V_q^2)}{(1 + \omega C^2 R^2)} \]

Where \( \omega \) is the angular frequency. This equation was obtained when the sample impedance is in series with a known resistance (1 kΩ), which is in parallel with the lock-in input impedance. \( R \) represents the equivalent resistance of the lock-in input resistance (100 MΩ) and the known resistance, \( C \) the lock-in input capacitance (15 pF), \( V_i \) the input signal (|\( V_i \)|=1 V), and \( V_f \) and \( V_q \) the “in-phase” and the “out-of-phase” components of the measured signal. The sample was modeled by a lumped circuit consisting of a resistance and a capacitor in parallel. The complex admittance \( Y^*(\omega) = 1/Z^*(\omega) = G(\omega) + j B(\omega) \) can be converted into complex permittivity formalism \( \varepsilon^*(\omega) = \varepsilon'(\omega) - j \varepsilon''(\omega) \) by the relations:

\[ \varepsilon'(\omega) = \frac{B(\omega) \varepsilon}{\varepsilon_0 A \omega} \]  \[ \varepsilon''(\omega) = \frac{G(\omega) \varepsilon}{\varepsilon_0 A \omega} \]

where \( A \) is the cross-sectional area of the sample, \( \varepsilon \) is its thickness and \( \varepsilon_0 \) is the permittivity of a vacuum (\( \varepsilon_0 = 8.85 \times 10^{-12} \) F m\(^{-1} \)). The terms \( G(\omega) \) and \( B(\omega) \) are respectively the conductance and the susceptance of the samples. Estimating relative errors on both real and imaginary part of the complex permittivity are: \( \Delta \varepsilon'/\varepsilon' < 10 \% \) and \( \Delta \varepsilon''/\varepsilon'' < 5 \% \).

Results and Discussion

X-ray and DSC analysis

The X-ray diffraction pattern shows no crystalline phases in the bioglass sample. Figure 1 presents the diffraction spectrum of the sample; this latter is amorphous as indicated by the absence of Bragg peaks and presence of amorphous halos.

Figure 2 shows the heating DSC thermogram of the bioglass sample. At about 420 K a change in the base line is observed. This phenomenon is attributed to the glass transition temperature \( T_g \). This measurement indicates that the glass transition temperature \( T_g \) which is associated to the transition from a glass like form to a rubbery. It should be reminded that the determination of \( T_g \) in our case, was carried out according to the method of the tangents. As, in general, a glass transition involves a small flow of heat, the detected variations of capacity calorific or enthalpy are also small, and for this, the determination is not very accurate.

Analysis of dielectric spectrum and modeling

The study of frequency dependent permittivity spectra is a well-established method for characterizing the hopping dynamics of ions. Frequency dependence on real (\( \varepsilon' \)) and imaginary (\( \varepsilon'' \)) parts of the effective dielectric permittivity \( \varepsilon^* \) spectra at various temperatures of the phosphosilicate bioglass composite containing 0.1SiO2-0.2CaO-0.2Na2O-0.5P2O5 are shown in Figure 3. The appearance of broad dielectric relaxations for temperature below \( T_g \) on the isothermal runs of the loss factor is presented in these measurements, as shown in Figure 3a, it is observed that the low-frequency value of \( \varepsilon' \) is high and the peak position is shifted to the high frequency side with increasing temperature. From aforementioned analysis, one can conclude that the
frequency region below the peak maximum of \( \varepsilon' \) determines the range in which charge carriers are mobile over long distances and in the region above the peak maximum the carriers are confined to potential wells being mobile over short distances [26,27].

For modeling these behaviors, we used the Nyquist diagram representation, as depicted in Figure 4a. The unsymmetrical profile of \( \varepsilon' \) indicates that the single relaxation time as described by the Debye equation is inappropriate for describing the electrical relaxation and should be replaced by Havriliak-Negami (HN) phenomenology [28]:

\[
\frac{\varepsilon'(\omega) - \varepsilon_{\infty}}{\varepsilon_s - \varepsilon_{\infty}} = \frac{1}{1 + (i\omega\tau)^\alpha}
\]

(1)

Where the positive constants \( \varepsilon_s \) and \( \varepsilon_{\infty} \) denote the static (\( \omega = 0 \)) and the high frequency values of the permittivity, respectively. \( \omega \) denotes the angular frequency (\( \omega = 2\pi f \)), \( \tau \) is the relaxation time of the composite, \( \alpha \) is the shape parameter representing symmetrical distribution of relaxation time and \( \beta \) is the shape parameter of an asymmetric relaxation curve. The maximum frequency of the relaxation peak in \( \varepsilon' \) (\( \omega \)) is approximately situated at \( 1/2\pi\tau \). The width parameter \( \alpha \) specifies the slope of the low frequency side of the relaxation and \( -\alpha\beta \) gives the slope of the high frequency side of the relaxation in \( \varepsilon''(\omega) \) [21].

The Havriliak-Negami (HN) equation includes the Debye model for \( (\alpha = \beta = 1) \), Cole-Cole model (CC) for \( (\beta = 1) \) and Cole-Davidson (CD) model for \( (\alpha = 1) \).

Our goal now is to assess with accuracy the behavior of \( \varepsilon'(\omega) \) according to the HN model. One of the most popular ansatz for the relaxation in dielectric materials is given by the HN phenomenology (Equation 1). Figure 4b shows an example of the \( (\varepsilon', \varepsilon'') \) vs. frequency and \( \varepsilon' \) vs. \( \varepsilon'' \) data along with a simulation (solid line) based on the HN modeling for the dielectric permittivity. The basic functional form of \( \varepsilon' \) is well known and can be expressed as:

\[
\frac{\varepsilon'(\omega) - \varepsilon_{\infty}}{\varepsilon_s - \varepsilon_{\infty}} = \frac{\cos(\beta\phi)}{1 + 2(\omega\tau)^\alpha \cos(\frac{\pi}{2}) + (\omega\tau)^{2\alpha}}
\]

(2)

\[
\frac{\varepsilon''(\omega)}{\varepsilon_s - \varepsilon_{\infty}} = \frac{\sin(\beta\phi)}{1 + 2(\omega\tau)^\alpha \cos(\frac{\pi}{2}) + (\omega\tau)^{2\alpha}}
\]

(3)

Where

\[
\phi = \tan^{-1}\left(\frac{(\omega\tau)^\alpha \sin(\frac{\pi}{2})}{1 + (\omega\tau)^{2\alpha}}\right)
\]

(4)

We performed a fit to the data using the Equations (2-4) for \( \varepsilon' \) and \( \varepsilon'' \) from which we extract the parameters \( \alpha \) and \( \beta \) which gauge the broadening of the loss spectrum. Figure 5 shows the evolutions of the relaxation parameters with temperature, it appears that the behavior of the parameters \( \alpha \) and \( \beta \) reveal that dielectric data are best fitted according to the CD model at low temperatures (\( T < 300 \) K) and according to the CC model for high temperatures (\( T > 350 \) K). The decrease of \( \alpha \) and increase of \( \beta \) with increasing of temperature indicating that the system departs from the Debye model this behavior is due to the changing dynamics of dipole clusters in low temperature and to alkali ion dynamics in network bioactive glasses. Indeed, the temperature-dependence of relaxation times reveals a steadily decreasing behavior due to an increase molecular dipoles mobility as temperature increases, for a higher temperature (\( T > 350 \) K), the relaxation time does not depend of temperature which indicate that the mechanism does not result simply from thermally activated dipolar interactions but may be also related to a cooperative effect of network modifiers (alkali ions).
The effective complex permittivity of bioactive glass composite was studied over a frequency range from 100 Hz to 1 MHz and in a temperature range from 100 to 370 K by impedance spectroscopy. This study exhibits typical dielectric relaxation process which was modelled using the Havriliak–Negami phenomenological. The analysis of the temperature dependence of their relaxation time using the Vogel-Tamman-Fulcher (VTF) model shows a weak interaction in the dielectric network.

**Conclusion**

The complex permittivity of bioactive glass composite is taken as indication of a phase-transition-like “ideal” glass transition that would occur at a temperature \(T_{\text{VF}}\) below the glass temperature \(T_g\) which, however, is avoided for dynamical reasons. It provides some support to theories that assume such a transition underlying the evolution of the glassy state [18,24].

The best fit of our data using maximum likelihood yields \(\tau_0 = 8.03 \times 10^{-9} \text{ s}\), \(T_{\text{VF}} = 220\text{K}\) which an ordering temperature lower than the \(T_g\) whose significances has remained unclear (there is no microscopic presentation to calculate \(T_g\)), and free energy of thermal activation energy \(W = 58.08 \text{ meV}\) with a correlation coefficient of \(R = 0.998\) which we interpret as the average potential barrier between different sites in the network heterostructure. The obtained value of \(W\) is very smaller than the data of Dutta et al. [29] such that the dielectric relaxation of the \(\text{Na}_2\text{O-CaO-Si}_2\text{O}\) system with various concentrations of alkali ions, this difference may be related to the effect of phosphate \((\text{P}_2\text{O}_5)\) that is added in this study, on the rigidity of network mesostructure which caused the decreases in activation energy.

**References**


